

Multi-stage On-Demand Program Slicing for Modular Analysis of Multi-threaded Programs

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Precise analysis of multi-threaded programs requires combining flow-sensitive pointer analysis (FSPTA) with interleaving and lock analysis (ILA) to reason about cross-thread value flows under feasible concurrent executions. ILA computes may-happen-in-parallel (MHP) relations and lock-release spans to determine when shared accesses can occur concurrently. Unfortunately, these analyses are both expensive and tightly coupled: FSPTA needs ILA to rule out infeasible inter-thread def-use relations, while ILA needs alias information to identify interference-relevant interactions. As a result, whole-program analyses often spend most of their time on code that is irrelevant to the client query. We present MSLI, an on-demand slicing framework for modular analysis of multi-threaded programs. It extracts compact, query-relevant program slices while preserving the answers of downstream analyses. Unlike single-pass slicing over a unified dependence graph, MSLI performs multi-stage slicing with analysis-specific criteria. Concretely, a lightweight pre-analysis establishes an over-approximation of inter-thread value flows and performs ILA slicing source extraction to identify the MHP and lock-span queries required later for ILA slicing. The refined main-phase ILA results then enable reconstruction of a thread-aware value-flow graph to guide FSPTA slicing, supporting modular analysis and downstream clients. We implement MSLI in SVF and evaluate it on ten large real-world projects with data race detection as a representative client. Compared with the unsliced baseline (FSAM), MSLI reduces the analyzed ICFG to 5.4% (ILA) and 25.7% (FSPTA), reduces ILA/FSPTA runtimes to 4.7%/18.3%, and cuts total analysis time to 20.8% on average, while producing identical query outcomes and race alarms.

CCS Concepts: • **Software and its engineering** → **Automated static analysis**; **Multithreading**; • **Theory of computation** → **Program analysis**.

Additional Key Words and Phrases: Program Slicing, Multi-Threaded Programs, Pointer Analysis

ACM Reference Format:

Jiawei Yang, Xiao Cheng, Jiawei Wang, Xiapu Luo, and Yulei Sui. 2026. Multi-stage On-Demand Program Slicing for Modular Analysis of Multi-threaded Programs. *Proc. ACM Softw. Eng.* 3, ISSTA, Article ISSTA164 (October 2026), 22 pages. <https://doi.org/10.1145/3832255>

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ACM 2994-970X/2026/10-ARTISSTA164

<https://doi.org/10.1145/3832255>

1 Introduction

Precise analysis of multi-threaded programs requires not only identifying memory locations that may be shared across threads, but also determining when such interactions can occur. Flow-sensitive pointer analysis [24] is therefore important for capturing the ordering of memory updates and improving the precision of cross-thread data-flow reasoning. Sparse flow-sensitive pointer analysis [9, 24, 40] further improves scalability by restricting the propagation of data-flow facts (points-to sets) along relevant def-use chains, thereby avoiding redundant propagation along control flows that do not affect pointer relationships.

In the presence of concurrency, constructing accurate def-use chains additionally requires *interleaving and lock analysis* (ILA) to determine which statements from different threads may execute concurrently. ILA comprises two components: (i) *interleaving analysis*, which computes may-happen-in-parallel (MHP) relations to identify statements that can execute simultaneously across threads, and (ii) *lock analysis*, which derives lock-release spans to determine when shared accesses are protected by common locks. FSAM [39] addresses this challenge by integrating sparse, flow-sensitive pointer analysis (FSPTA) with ILA results. In particular, FSAM leverages MHP relations and lock spans to conservatively construct a value-flow graph that captures feasible inter-thread def-use relationships, while pruning spurious connections arising from infeasible thread interleavings or mutually exclusive lock-protected regions. Subsequent work has focused on improving the scalability of flow-sensitive pointer analysis [9, 42] and interleaving and lock analysis [54]. For example, Li et al. [9] enhance pointer analysis efficiency by merging similar pointer abstractions, whereas Zhou et al. [54] propose an MHP analysis based on vector clocks. Despite these advances, whole-program analyses often spend most of their time on code that is irrelevant to the client query. This motivates the need for techniques that can reduce the analysis scope while preserving precision for queries of interest.

Our goal is **on-demand program slicing for modular analysis of multi-threaded programs**: given slicing targets specified by users or, as in our experiments, derived from pre-analysis (e.g., potential race pairs), we want to retain only the code relevant to those targets while preserving (i) inter-thread value flows enabled by pointer/alias information from FSPTA and (ii) feasible interleavings and synchronization constraints captured by ILA. This enables modular analysis: instead of running whole-program FSPTA and ILA over the entire codebase, we reduce the analyzed ICFG/value-flow graph to what is strictly necessary for the module or query at hand, without sacrificing precision where it matters.

An intuitive approach is to apply program slicing to **eliminate statements irrelevant to the downstream client queries**, thereby accelerating both FSPTA and ILA while preserving precision. Prior concurrent-program slicing techniques mainly model cross-thread interference and synchronization dependencies [28, 32, 45], but, to our knowledge, do not separately construct analysis-specific slices for jointly accelerating FSPTA and ILA. Inspired by existing data and synchronization dependence formulations [28, 32], we construct a new, straightforward single-pass baseline that unions these dependences and computes one slice. We refer to this baseline as *single-pass slicing*.

While this single-pass slicing strategy safely over-approximates the dependencies needed by both analyses, it often yields slices that are larger than necessary. This is because the unified dependency graph conservatively combines all dependencies required by FSPTA and ILA, thereby collapsing analysis-specific dependencies into a single solution. As a result, dependencies that are required only under either inter-thread or value-flow conditions are treated as universally necessary during slicing. This loss of distinction forces the slicing process to retain statements that are not simultaneously required for both analyses under the same execution context, leading to

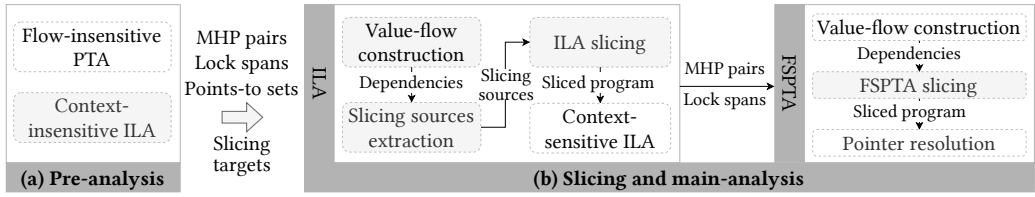


Fig. 1. Framework overview of multi-stage slicing.

slices that are larger than necessary. Consequently, the resulting slice may still contain extraneous code that does not impact the specific queries of either analysis, thereby limiting the potential efficiency gains. This observation motivates the need for a more refined slicing strategy that can **tailor program slices to the distinct requirements of FSPTA and ILA**, thereby producing smaller and more effective slices.

However, separately slicing the program for FSPTA and ILA is non-trivial due to their differing dependency requirements and mutual interdependence. FSPTA depends on ILA results to determine feasible inter-thread def-use relations: MHP information identifies which stores and loads may execute concurrently, while lock spans prune infeasible value flows between mutually exclusive regions. Conversely, slicing for ILA must account for inter-thread aliasing identified by pointer analysis in order to accurately determine which statements may interfere and, consequently, to identify appropriate slicing criteria. Ignoring these interdependencies, for example, by conservatively assuming that all statements from different threads may interleave, would introduce excessive imprecision, resulting in overly conservative value-flow connections. This, in turn, degrades the effectiveness of the slicing for FSPTA and undermines the scalability of the subsequent main analysis phases.

To address these challenges, we introduce MSLI, a novel slicing technique for on-demand modular analysis of multi-threaded programs. The key idea is to perform multi-stage slicing, in which **slicing is carried out incrementally using analysis-specific criteria** rather than producing a single slice that simultaneously satisfies the requirements of both FSPTA and ILA. Specifically, to relax the tight interdependence between the two analyses, MSLI first applies an imprecise but fast interleaving and lock analysis as a preliminary stage. This initial analysis, together with a flow-insensitive Andersen-style pointer analysis [7], identifies an over-approximation of inter-thread value flows, which is sufficient to determine the slicing criteria for the subsequent ILA slicing phase. The refined ILA then provides precise MHP relations and lock spans that enable the construction of a more accurate inter-thread value-flow graph, which guides the FSPTA slicing phase, ensuring that only statements relevant to feasible inter-thread interactions are retained.

Figure 1 presents the pre-analysis phase (Figure 1(a)) and the slicing and main-analysis phase (Figure 1(b)) of our on-demand multi-stage slicing framework. The framework takes LLVM intermediate representation (LLVM IR) as input and leverages a static analysis tool, SVF [40], to construct an interprocedural control-flow graph and a call graph. It then performs a lightweight pre-analysis consisting of flow-insensitive Andersen-style pointer analysis and context-insensitive interleaving and lock analysis, together with the extraction of data dependences (value-flow edges) and synchronization dependences. Based on the resulting dependency information, the framework conducts an ILA slicing phase that incorporates both data and synchronization dependences. Prior to this slicing step, the preliminary pointer and interleaving analyses construct an over-approximation of inter-thread value flows and perform ILA slicing source extraction to identify the MHP and lock-span queries required by subsequent analyses. This ensures that statements necessary for resolving these queries are preserved during slicing, even before precise inter-thread value-flow construction. Finally, the framework performs FSPTA slicing guided by data dependences derived from a reconstructed, thread-aware value-flow graph, which is built using refined, context-sensitive

MHP relations and lock spans obtained from ILA. Sparse, flow-sensitive pointer analysis is then executed on the resulting sliced value-flow graph.

In summary, this paper makes the following contributions:

- We propose MSLI, an on-demand, multi-stage slicing framework for modular analysis of multi-threaded programs. It decouples the tight interdependence between flow-sensitive pointer analysis (FSPTA) and interleaving and lock analysis (ILA) by progressively refining analysis-specific slicing criteria, avoiding the excessive conservatism of single-pass slicing while preserving downstream query results.
- We formalize slicing correctness as preservation of downstream-relevant ILA predicates (MHP relations and lock spans) and FSPTA alias answers, and show that our sliced ICFG reconstruction preserves required reachability and contexts.
- We implement MSLI in SVF [40] and evaluate it on ten large projects, demonstrating that the resulting slices accelerate modular FSPTA and preserve client results with data race detection as a representative client. Compared with the unsliced baseline (FSAM), MSLI reduces the analyzed ICFG to 5.4% (ILA) and 25.7% (FSPTA), reduces ILA/FSPTA runtimes to 4.7%/18.3%, and cuts total analysis time to 20.8% on average, while producing identical query outcomes and race alarms.

2 Preliminaries and Problem Formulation

This section provides the necessary background on the FSAM framework [39], a representative flow-sensitive pointer analysis (FSPTA) framework for multi-threaded program analysis. Building upon this foundation, we then present a formal problem formulation that characterizes the objectives of our approach.

2.1 FSAM Overview

FSAM begins by performing a flow-insensitive Andersen-style pointer analysis to compute preliminary points-to information. This information is then used to perform ILA (§2.3), which derives concurrency information about thread interactions. Subsequently, both the points-to and concurrency results are leveraged to construct thread-aware value-flow graphs, which enable the execution of FSPTA (§2.4). FSAM does not incorporate program slicing. It applies both FSPTA and ILA to the entire program, analyzing all statements and control-flow paths.

2.2 Abstract Thread Model

This section presents the abstract thread model employed by FSAM. We formalize the notions of abstract threads, intra-thread control-flow graphs, and the thread-relation model that underpin the analysis.

Abstract threads. We use *abstract thread* to approximate *concrete thread* during actual program execution. An abstract thread t represents either the initial entry thread originating from `main` or a library entry point, or a context-sensitive invocation of `pthread_create` at a fork site. Each abstract thread may correspond to one or multiple runtime thread instances. When an abstract thread corresponds to multiple spawning events, for instance, under different calling contexts or due to loops or recursion, it is classified as a *multi-forked thread*.

Intra-thread control-flow graph ($ICFG_t$). ILA is formulated as a data-flow analysis operating over the collection of $ICFG_t$. Each abstract thread t is associated with a corresponding $ICFG_t$. Intra-procedural edges, denoted $s \xrightarrow{\text{intra}} s'$, capture sequential control flow within a procedure. Inter-procedural edges model procedure calls and returns: call edges $s \xrightarrow{\text{call}_i} s'$ connect a call node

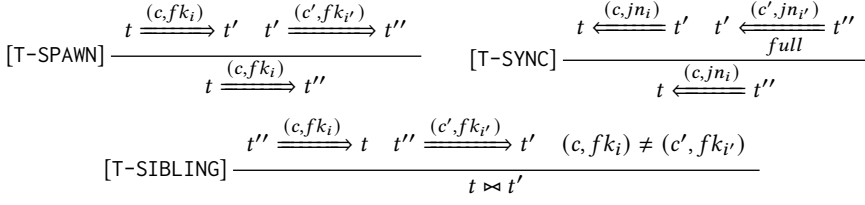


Fig. 2. Inference rules for deriving thread relations.

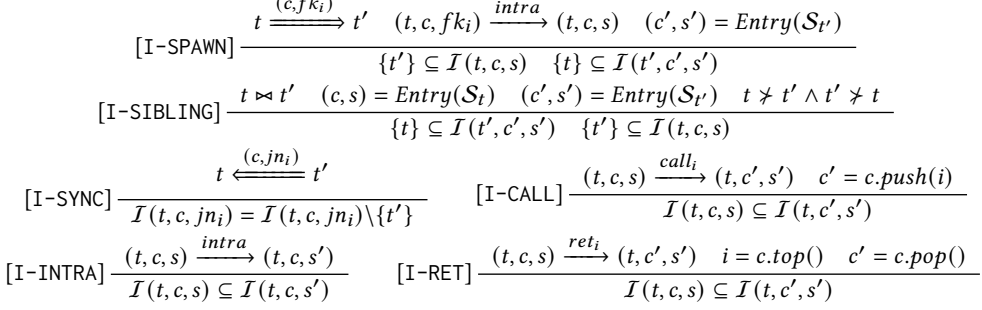


Fig. 3. Inference rules for interleaving analysis [39].

s to the entry statement s' of the callee at callsite i , while return edges $s \xrightarrow{\text{ret}_i} s'$ connect the exit statement s of the callee to the corresponding return node s' at the same callsite. Callsites to `pthread_create` and `pthread_join` connect their call nodes directly to the corresponding return nodes via intra-procedural edges.

Thread relation model. Figure 2 formalizes three fundamental relations over abstract threads.

The *spawning relation* $t \xrightarrow{(c, fk_i)} t'$ indicates that thread t spawns thread t' at fork site fk_i under call string context c , either directly or transitively. The *synchronization relation* $t \xleftarrow{(c, jn_i)} t'$ indicates that spawned thread t' joins with its spawner t at join site (c, jn_i) , provided the corresponding fork and join thread handles have the same singleton pre-analysis points-to set and t' is not multi-forked. Synchronization may be direct or transitive, but transitive synchronization requires all intermediate joins to be full joins. Two threads t and t' are *siblings*, written $t \bowtie t'$, if they share a common spawner and neither spawns the other. A *happens-before* relation $t > t'$ holds when a join site that joins t dominates the fork site of t' .

2.3 Interleaving and Lock Analysis (ILA)

ILA comprises two components: interleaving analysis, which computes may-happen-in-parallel (MHP) information for statements, and lock analysis, which derives lock spans.

Interleaving analysis. Interleaving analysis is formulated as a data-flow analysis that operates flow- and context-sensitively over the $ICFG_t$ s of all threads. For a statement s in thread t 's $ICFG_t$, the analysis approximates which threads may execute in parallel with t at the program point where s is executed. We denote this interleaving state as $\mathcal{I}(t, c, s)$, where c is the calling context that distinguishes the specific instance of s when its enclosing method is invoked under context c .

Figure 3 presents the inference rules for interleaving analysis. Each thread t forked at (c, fk_i) is associated with a start procedure $\mathcal{S}_t$, whose entry statement is given by $\text{Entry}(\mathcal{S}_t) = (c', s)$ with context $c' = c.\text{push}(i)$. Rule [I-SPAWN] adds interleaving states for the statement following the fork

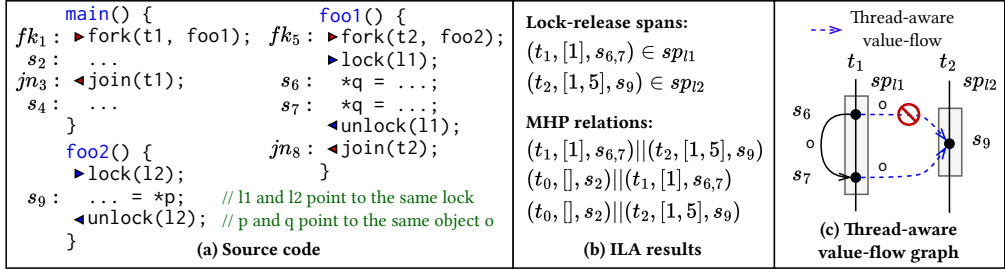


Fig. 4. An example of ILA and FSPTA.

site and the spawned thread's entry. Rule [I-SIBLING] adds interleaving states to sibling threads' entry statements. Rule [I-SYNC] removes interleaving states after join sites. Rules [I-CALL], [I-INTRA], and [I-RET] propagate interleaving states along intra-thread control flows. We write $(t_1, c_1, s_1) || (t_2, c_2, s_2)$ to denote that statement s_1 in thread t_1 under context c_1 may happen in parallel with statement s_2 in thread t_2 under context c_2 . This holds if either (1) $t_1 \neq t_2$ and $t_2 \in \mathcal{I}(t_1, c_1, s_1) \wedge t_1 \in \mathcal{I}(t_2, c_2, s_2)$, or (2) $t_1 = t_2$ and t_1 is multi-forked.

Lock analysis. Lock analysis computes lock-release spans (Definition 1) for context-sensitive lock sites by performing a flow- and context-sensitive analysis over lock/unlock operations, guided by the points-to information obtained from pre-analysis.

Definition 1 (Lock-Release Spans). A lock-release span sp_l at a lock site $(t, c, lock(l))$ is defined as the set of statements in $ICFG_t$ reachable from $(c, lock(l))$ to its matching release site $(c', unlock(l'))$, computed via forward reachability where calls and returns are matched context-sensitively. The span is considered valid if and only if l and l' have the same singleton pre-analysis points-to set, which establishes the must-alias relation $l \equiv l'$.

Example 1. Figure 4 illustrates both interleaving analysis and lock analysis. Two lock-release spans, sp_{l1} and sp_{l2} , are protected by a common lock, since $l1$ and $l2$ are identified as must-aliases. The program exhibits two immediate fork relations: $t_0 \xrightarrow{([],fk_1)} t_1$ and $t_1 \xrightarrow{([1],fk_5)} t_2$.

By transitivity, we obtain the spawning relation $t_0 \xrightarrow{([],fk_1)} t_2$. Consequently, the MHP relation $(t_1, [1], s_6) || (t_2, [1, 5], s_9)$ holds. Since the join site jn_8 is a full join, a synchronization relation $t_0 \xleftarrow{([],jn_3)} t_2$ is established, which ensures that $(t_0, [], s_4) \not|| (t_2, [1, 5], s_9)$.

2.4 Sparse Flow-Sensitive Pointer Analysis (FSPTA)

Building upon the ILA results and the pre-analysis points-to information, we construct a thread-aware value-flow graph and subsequently perform sparse pointer resolution over this graph.

Thread-aware value-flow construction. The construction of value flows proceeds in two stages. In the first stage, thread-oblivious value flows are established using only the points-to information obtained from pre-analysis [39]. In the second stage, we incorporate *thread-aware* value flows by leveraging both points-to and concurrency information. Specifically, for each pair of MHP store-load or store-store statements $(t, c, s) || (t', c', s')$, we introduce a thread-aware value-flow edge $s \xrightarrow{o} s'$ for each object $o \in AS(p, q)$, where $AS(p, q)$ denotes the intersection of the points-to sets derived from pre-analysis. This construction is formalized by the following rule:

$$[\text{THREAD-VF}] \frac{s : *p = _ \quad s' : _ = *q \quad \text{or} \quad s' : *q = _ \quad (t, c, s) \parallel (t', c', s') \quad o \in AS(p, q)}{s \xrightarrow{o} s'}$$

Subsequently, we compute *non-interference lock pairs* to refine the [THREAD-VF] rule by excluding value flows whose endpoints form non-interference lock pairs under all contexts.

Definition 2 (Non-Interference Lock Pairs). For an object $o \in \mathcal{A}$ and a lock span sp_l , we define the *span head* and *span tail* as follows:

$$HD(sp_l, o) = \{(t, c, s) \in sp_l \mid \nexists (t', c', s') \in sp_l : s' \xrightarrow{o} s\},$$

$$TL(sp_l, o) = \{(t, c, s) \in sp_l \mid s \text{ is a store} \wedge \nexists (t', c', s') \in sp_l : (s' \text{ is a store} \wedge s \xrightarrow{o} s')\}.$$

Let $(t, c, s) \parallel (t', c', s')$ be an MHP statement pair, where s is a store. Suppose both statements are protected by at least one common lock, i.e., there exist locks l and l' such that $(t, c, s) \in sp_l$, $(t', c', s') \in sp_{l'}$, and $l \equiv l'$. We say that the pair forms a *non-interference lock pair* if $(t, c, s) \notin TL(sp_l, o)$ or $(t', c', s') \notin HD(sp_{l'}, o)$ holds.

Example 2. We revisit the example in Figure 4 to illustrate the thread-aware value-flow construction process. Figure 4(c) depicts the resulting graph. Since $(t_1, [1], s_i) \parallel (t_2, [1, 5], s_9)$ for $i \in \{6, 7\}$ and $o \in AS(p, q)$, two candidate thread-aware value-flow edges, $s_6 \xrightarrow{o} s_9$ and $s_7 \xrightarrow{o} s_9$, are initially introduced. However, according to lock analysis, $(t_1, [1], s_6) \notin TL(sp_{l_1}, o)$, which implies that $(t_1, [1], s_6)$ and $(t_2, [1, 5], s_9)$ constitute a non-interference lock pair. Consequently, the value flow $s_6 \xrightarrow{o} s_9$ is removed. In contrast, $(t_1, [1], s_7) \in TL(sp_{l_1}, o)$ and $(t_2, [1, 5], s_9) \in HD(sp_{l_2}, o)$, so the corresponding value flow $s_7 \xrightarrow{o} s_9$ is preserved.

Sparse pointer resolution. We apply the Andersen-style sparse pointer resolution method for sequential programs [39] to the constructed thread-aware value-flow graph to derive over-approximated points-to results.

2.5 Problem Formulation

Definition 3 (Query Preservation for ILA and FSPTA). Let P'_{ILA} and P'_{FSPTA} be the sliced programs for ILA and FSPTA, respectively. Let $\llbracket \varphi \rrbracket_P$ denote the answer to query φ on program P . The downstream task specifies a set of context-sensitive statement instances $CSS_{ILA} \subseteq T \times C \times S$ for ILA queries and a set of variables VAR_{FSPTA} for alias queries. Slicing preserves ILA and FSPTA queries if (i) for any $(t_1, c_1, s_1), (t_2, c_2, s_2) \in CSS_{ILA}$, $\llbracket (t_1, c_1, s_1) \parallel (t_2, c_2, s_2) \rrbracket_{P'_{ILA}} = \llbracket (t_1, c_1, s_1) \parallel (t_2, c_2, s_2) \rrbracket_P$, (ii) for any $(t, c, s) \in CSS_{ILA}$ and any corresponding lock-release span sp_l , $\llbracket (t, c, s) \in sp_l \rrbracket_{P'_{ILA}} = \llbracket (t, c, s) \in sp_l \rrbracket_P$, and (iii) for any $v_1, v_2 \in VAR_{FSPTA}$, $\llbracket AS(v_1, v_2) \rrbracket_{P'_{FSPTA}} = \llbracket AS(v_1, v_2) \rrbracket_P$.

We formalize the goal of our slicing approach as query preservation between the original program and its sliced counterparts:

Given a multi-threaded program P and a downstream analysis task (e.g., data race detection) that requires both ILA and FSPTA results, our goal is to compute two sliced programs P'_{ILA} and P'_{FSPTA} such that both slices preserve all query results required by the downstream task, as formalized in Definition 3, and the combined cost of performing ILA on P'_{ILA} and FSPTA on P'_{FSPTA} is substantially lower than performing these analyses on the original program P .

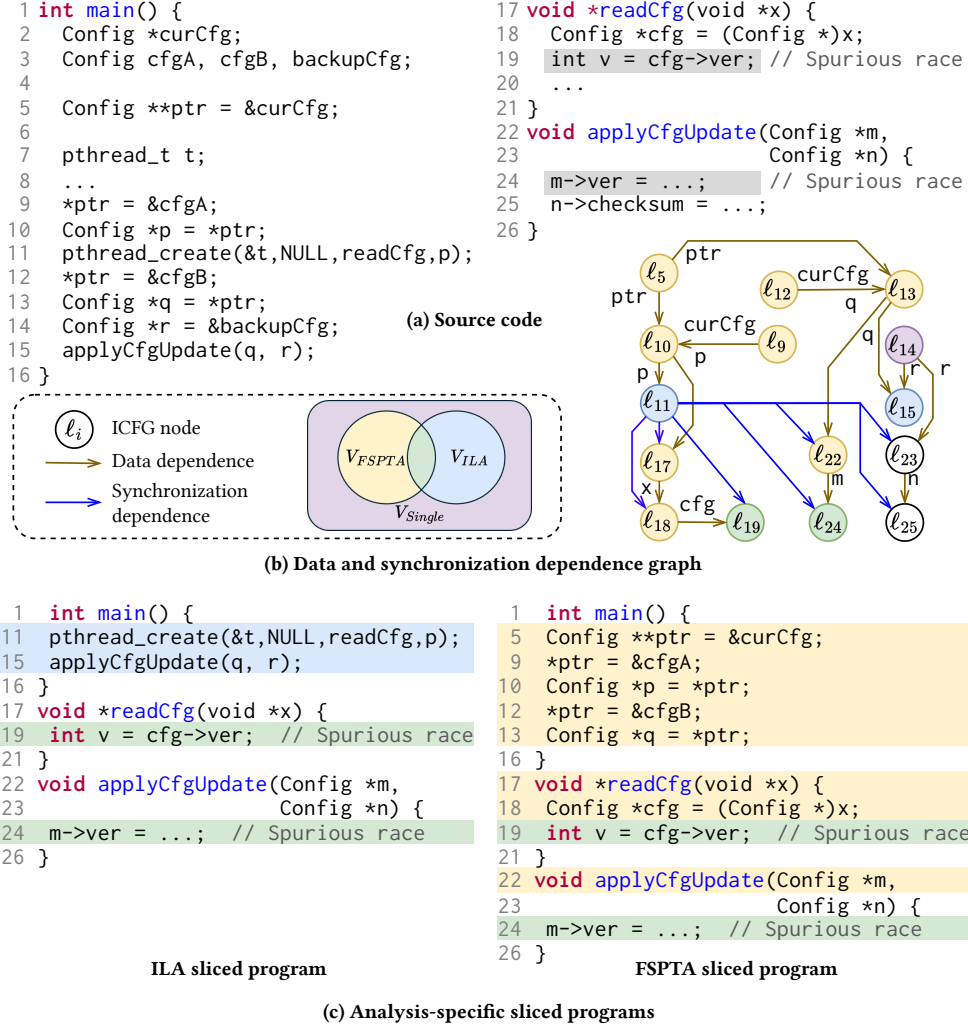


Fig. 5. A motivating example with (a) the original program, (b) its combined dependence graph and slice regions, and (c) the sliced programs for ILA and FSPTA.

3 A Motivating Example

Figure 5(a) presents a real-world configuration-management scenario involving concurrent reads and updates. The program comprises a main thread that spawns a worker thread to execute `readCfg`. Prior to spawning, the main thread assigns the address of `cfgA` to `curCfg` at l_9 and passes this address as the thread argument via pointer `p`. Within `readCfg`, the worker thread (created at l_{11}) reads the `ver` field of `cfgA` at l_{19} . Subsequently, after spawning the worker thread, the main thread updates `curCfg` to point to `cfgB` at l_{12} and invokes `applyCfgUpdate`, passing the addresses of `cfgB` and `backupCfg` via pointers `q` and `r`, respectively. This function then writes to both `cfgB` and `backupCfg` at l_{24} and l_{25} , respectively.

Under the standard definition of a data race [11, 17, 20], the program contains no race because the main thread and worker thread access distinct objects, `cfgB` and `cfgA`, respectively. However, a flow-insensitive pointer analysis cannot distinguish between the two assignments to `curCfg` at

ℓ_9 and ℓ_{12} . Consequently, it conservatively concludes that p and q may alias and potentially refer to either cfgA or cfgB . This imprecision leads to a spurious race warning between the read at ℓ_{19} and the write at ℓ_{24} . In contrast, a flow-sensitive pointer analysis correctly infers that p points exclusively to cfgA while q points exclusively to cfgB , thereby eliminating the false positive.

Motivation. While sparse flow-sensitive pointer analysis achieves high precision, it remains computationally expensive for large-scale codebases [9, 24]. For downstream clients such as race detection, a large portion of the program is *irrelevant to the analysis query*: analyzing these statements does not influence the final result. For instance, statements such as ℓ_{23} and ℓ_{25} do not contribute to determining the race detection outcome, as the write to backupCfg at ℓ_{25} does not race with any statement in other threads. This observation motivates the application of program slicing to eliminate irrelevant code, thereby accelerating the subsequent interleaving and lock analysis (ILA) and flow-sensitive pointer analysis (FSPTA) stages.

Single-Pass Slicing. A straightforward baseline approach constructs both data dependences and synchronization dependences [28, 32], then computes a single-pass slice over the unified dependence graph. Figure 5(b) illustrates this combined dependence graph for the example program, where data dependences are denoted as $\xrightarrow{\text{data}}$ and synchronization dependences as $\xrightarrow{\text{sync}}$. The region labeled V_{Single} in the figure represents the result of this single-pass slicing method. However, ILA and FSPTA require distinct program subsets to achieve both precision and soundness. Specifically, certain statements are essential for ILA but irrelevant to FSPTA, while others are crucial for FSPTA but unnecessary for ILA. For instance, ℓ_{11} serves as a synchronization primitive that enables ILA to determine the may-happen-in-parallel relation between ℓ_{19} and ℓ_{24} , and ℓ_{15} is essential for context management. Neither statement contributes to pointer resolution for cfg at ℓ_{19} or m at ℓ_{24} , rendering them irrelevant to FSPTA. Conversely, statements such as ℓ_{10} and ℓ_{13} are critical for propagating pointer information in FSPTA but do not affect the concurrency analysis performed by ILA. Furthermore, merging these dependencies into a single slice V_{Single} introduces additional statements (colored purple) that are not required by either analysis (e.g., ℓ_{14}). This over-approximation leads to inefficiencies in both analysis stages. These observations motivate the design of a multi-stage slicing technique that separately accelerates ILA and FSPTA by computing tailored slices for each analysis stage.

Our Approach. Rather than computing a single slice over the combined dependence graph, we propose a multi-stage slicing approach that decouples the analysis into two distinct stages, each tailored to its specific dependence requirements. We identify target statements that require exclusively ILA results and those that require exclusively FSPTA results, then compute slices based on their respective dependences: data dependence for FSPTA, and synchronization and call dependences for ILA. In this example, the race statements necessitate ILA information to determine concurrency relations, while the pointer values accessed by these statements require FSPTA information for precise alias resolution. Figure 5(c) shows the resulting programs, with ℓ_{19} and ℓ_{24} shown in both listings as the query sites. For these queries, the ILA slice retains synchronization and call structure with reconstructed function boundaries, while the FSPTA slice retains the pointer flow needed to resolve the accessed objects.

Our multi-stage slicing approach yields tighter slices for both ILA and FSPTA compared to the single-pass approach. First, each stage operates on a smaller subgraph than the single-pass slice ($V_{\text{ILA}} \subseteq V_{\text{Single}}$ and $V_{\text{FSPTA}} \subseteq V_{\text{Single}}$), as each slice retains only the statements relevant to its respective analysis. Second, statements that are irrelevant to both analyses (e.g., ℓ_{14}) are eliminated entirely, thereby reducing the overall volume of code that must be analyzed across all stages.

4 Approach

MSLI begins with a lightweight pre-analysis to identify *slicing targets*, then performs ILA slicing (§4.2) to retain statements affecting concurrency analysis, followed by FSPTA slicing (§4.3) to retain statements affecting pointer resolution in the main-phase analyses.

4.1 Pre-Analysis

Pre-analysis uses flow-insensitive Andersen-style pointer analysis [7] to provide points-to information. It also uses context-insensitive ILA (details in §2.3) to provide concurrency information for the main phase. It identifies potential slicing targets. For instance, in data race detection, race pairs constitute the slicing targets. We denote a potential race pair as $(s, s') \in \text{RacePairs}_{pre}$, where s and s' are may-happen-in-parallel memory access statements (with at least one being a write) that access the same memory location without proper synchronization in at least one thread pair.

4.2 ILA Slicing

ILA slicing retains a reduced, query-relevant set of statements while preserving the required ILA results. The process proceeds in three steps: (i) extracting slicing sources that may be queried by downstream analysis, (ii) performing synchronization-dependence slicing to retain relevant synchronization primitives, and (iii) performing call-dependence slicing to recover the calling contexts of the retained statements. Finally, we reconstruct a sliced ICFG by removing non-retained nodes and adding bridge edges over the remaining intraprocedural control flow.

ILA slicing source extraction. The slicing sources comprise not only the race statements identified during pre-analysis, but also statements that contribute to determining *thread-aware* value flows during value-flow construction in the subsequent FSPTA, thereby requiring concurrency information. Figure 6 summarizes the extraction rules.

$$[\text{INIT}] \frac{(s, s') \in \text{RacePairs}_{pre}}{\{s, s'\} \subseteq V_{ILA}} \quad [\text{THREAD-VF}] \frac{s \xrightarrow{o} s' \in \text{ThreadVF}(G'_{VFG})}{\text{Query}(s \xrightarrow{o} s') \subseteq V_{ILA}}$$

Fig. 6. Inference rules for ILA slicing source extraction.

Rule [INIT] directly includes all statements in RaceStmt_{pre} , as these statements may be queried during the final race detection phase. Rule [THREAD-VF] extracts the statements that will be queried for ILA information during thread-aware value-flow construction in the subsequent FSPTA (see Section 2.4). To construct thread-aware value flows, we first build a thread-aware value-flow graph VFG_{pre} using the ILA information obtained from pre-analysis. Since VFG_{pre} may contain value flows that are ultimately unused in the subsequent FSPTA (after FSPTA slicing is applied), we extract a sliced graph VFG'_{pre} based on the same criterion employed in FSPTA slicing (Section 4.3). We denote by $\text{ThreadVF}(VFG'_{pre})$ the set of thread-aware value-flow edges constructed on VFG'_{pre} . For each remaining thread-aware value-flow edge $s \xrightarrow{o} s'$, we define $\text{Query}(s \xrightarrow{o} s')$ as the set of statements that must be queried to determine the validity of this edge:

$$\text{Query}(s \xrightarrow{o} s') = \{s, s'\} \cup \bigcup_{((t, s), (t', s')) \in \text{InstPair}(s, s')} \pi\left(\text{Query}_o((t, s), (t', s'))\right),$$

where $\text{InstPair}(s, s') = \{((t, s), (t', s')) \mid (t, s) \parallel (t', s')\}$ denotes the set of may-happen-in-parallel instance pairs identified during pre-analysis, with each instance being a pair consisting of a thread and a statement. The projection $\pi(X) = \{x \mid \exists t : (t, x) \in X\}$ extracts the statement component from each instance.

$$\begin{array}{l}
\text{[D-SPAWN]} \frac{t \xrightarrow{fk_i} t' \quad (t, fk_i) \xrightarrow{\text{intra}} (t, s) \quad s' = \text{Entry}(S_{t'}) \quad FKS = \text{Prim}(t \xrightarrow{fk_i} t')}{FKS \subseteq \mathcal{D}(s) \quad FKS \subseteq \mathcal{D}(s')} \\
\text{[D-SIBLING]} \frac{t \bowtie t' \quad s = \text{Entry}(S_t) \quad s' = \text{Entry}(S_{t'}) \quad t \not\bowtie t' \wedge t' \not\bowtie t \quad FKS = \text{Prim}(t \bowtie t')}{FKS \subseteq \mathcal{D}(s) \quad FKS \subseteq \mathcal{D}(s')} \\
\text{[D-SYNC]} \frac{t \xleftarrow{c, jn_i} t' \quad JNS = \text{Prim}(t \xleftarrow{c, jn_i} t')}{JNS \subseteq \mathcal{D}(jn_i)} \quad \text{[D-INTRATD]} \frac{(t, s) \rightarrow (t, s')}{\mathcal{D}(s) \subseteq \mathcal{D}(s')}
\end{array}$$

Fig. 7. Rules for deriving synchronization dependencies in interleaving analysis.

For each instance pair, we collect all relevant witness instances within the corresponding lock-release spans:

$$Query_o((t, s), (t', s')) = \bigcup_{(t', s') \in sp_{t'}} (Pred_{sp_{t'}}(t', s', o)) \cup \bigcup_{(t, s) \in sp_l} (Succ_{sp_l}(t, s, o))$$

where

$$\begin{aligned}
Pred_{sp_{t'}}(t', s', o) &= \left\{ (t', x) \in sp_{t'} \mid x \xrightarrow{o} s' \right\}, \\
Succ_{sp_l}(t, s, o) &= \left\{ (t, x) \in sp_l \mid x \text{ is a store} \wedge s \xrightarrow{o} x \right\}.
\end{aligned}$$

Intuitively, $Pred_{sp_{t'}}(t', s', o)$ and $Succ_{sp_l}(t, s, o)$ provide the intra-thread witnesses necessary to determine membership in $HD(sp_{t'}, o)$ and $TL(sp_l, o)$, respectively. These membership tests, in turn, determine the outcome of the non-interference lock-pair test and consequently establish whether the thread-aware value flow exists. To ensure soundness, lock-release spans are computed conservatively (i.e., as may-spans), thereby accounting for all potential non-interference cases.

Synchronization-dependence slicing. Given the slicing sources, we perform synchronization-dependence slicing to retain the relevant *synchronization primitives* in the slice, that is, concurrency-related statements (including fork/join for interleaving analysis and lock/unlock for lock analysis) that may affect the interleaving behavior of other statements.

Figure 7 presents the rules for deriving synchronization primitives for interleaving analysis. These rules mirror the derivations in Figure 3, with each rule collecting the synchronization primitives on which its derivation depends. We summarize the collected dependencies using a function $\mathcal{D} : S \rightarrow 2^S$, where $\mathcal{D}(s)$ denotes the set of synchronization primitives on which statement s depends. Rules [D-SPAWN] and [D-SIBLING] extract the fork sites that witness spawning and sibling relationships among threads, while Rule [D-SYNC] collects join sites required to establish potential joining relations. Together, these rules capture the synchronization primitives that affect the interleaving behavior of the involved statements. Rule [D-INTRATD] propagates these dependencies along intra-thread control-flow edges.

The function $\text{Prim}(t R t')$ extracts the synchronization primitives that witness a thread relation $R \in \{\xrightarrow{fk_i}, \xleftarrow{jn_i}, \bowtie\}$ (Section 2.2) between abstract threads t and t' . Prim is defined as follows:

$$\text{Prim}(t R t') = \begin{cases} \{fk_i\} \cup \{fk_{t'} \mid \exists t'' : t \xrightarrow{fk_i} t'' \wedge t'' \xrightarrow{fk_{t'}} t'\} & R = \xrightarrow{fk_i}, \\ \{jn_i\} \cup \{jn_{t'} \mid \exists t'' : t \xleftarrow{jn_i} t'' \wedge t'' \xleftarrow{full, jn_{t'}} t'\} & R = \xleftarrow{jn_i}, \\ \text{Prim}(t'' \xrightarrow{fk_i} t') \cup \text{Prim}(t'' \xrightarrow{fk_{t'}} t) & R = \bowtie, \exists t'' : t'' \xrightarrow{fk_i} t' \wedge t'' \xrightarrow{fk_{t'}} t. \end{cases}$$

Algorithm 1: Sliced ICFG construction algorithm.**Input:** $G(V, E)$: Original ICFG, where $E = E_{\text{intra}} \uplus E_{\text{call}} \uplus E_{\text{ret}}$ $V_{\text{ILA}}^{\text{final}}$: Final ILA slice of the program**Output:** $G'(V', E')$: Sliced ICFG of the program

```

1 Function Slice( $G, V_{\text{ILA}}^{\text{final}}$ ):
2    $F' := \{\text{fun}(v) \mid v \in V_{\text{ILA}}^{\text{final}}\};$ 
3    $V' := V_{\text{ILA}}^{\text{final}} \cup \{\text{entry}_f, \text{exit}_f \mid f \in F'\};$ 
4    $E' := \emptyset; \quad V_{\text{del}} := \emptyset;$ 
5    $E_{\text{br}} := \{(\text{call}_i, \text{ret}_i) \mid \exists f \in \text{Callee}(i) : \text{entry}_f \notin V'\};$ 
6   // Construct bridge edges using only local control flow
7   foreach  $v_{\text{del}} \in V \setminus V'$  do
8     foreach  $v' \rightarrow v_{\text{del}} \in E_{\text{intra}} \cup E_{\text{br}} \wedge v' \notin V_{\text{del}}$  do
9       foreach  $v_{\text{del}} \rightarrow v'' \in E_{\text{intra}} \cup E_{\text{br}} \wedge v'' \notin V_{\text{del}}$  do
10        if  $v' \in V' \wedge v'' \in V'$  then
11           $E'.\text{insert}((v', v''));$ 
12        else
13           $E_{\text{br}}.\text{insert}((v', v''));$ 
14       $V_{\text{del}}.\text{insert}(v_{\text{del}});$ 
15  // Retain original edges and completed bridge edges
16  foreach  $e \in E \cup E_{\text{br}}$  do
17    if  $e.\text{src} \in V' \wedge e.\text{dst} \in V'$  then
18       $E'.\text{insert}(e);$ 
19  return  $G'(V', E');$ 

```

Synchronization primitives for lock analysis are obtained directly from pre-analysis results. Based on the may-lock results, we derive synchronization primitives by including all relevant lock statements and their matching unlock statements. Formally, for any statement $s \in S$, if s may be protected by a lock-release span sp_l , then we include the corresponding lock and unlock sites in its dependency set:

$$\forall s \in S, \forall l, l' : (\exists t : (t, s) \in sp_l) \wedge l \equiv l' \Rightarrow \text{lock}(l) \in \mathcal{D}(s) \wedge \text{unlock}(l') \in \mathcal{D}(s).$$

Given the dependence function $\mathcal{D}$, we extend the slicing sources with their synchronization-dependence witnesses to derive the augmented slice:

$$V_{\text{ILA}}^{\text{sync}} = V_{\text{ILA}} \cup \{s_d \mid s \in V_{\text{ILA}} \wedge s_d \in \mathcal{D}(s)\}.$$

Call-dependence slicing. Finally, we perform call-dependence slicing to recover the call sites necessary for preserving the calling contexts of the involved statements. We compute backward reachability on the call graph, starting from functions that contain statements in $V_{\text{ILA}}^{\text{sync}}$, to collect all call sites along the reachable paths. Let $CS(V_{\text{ILA}}^{\text{sync}})$ denote the set of such call sites. For each call site $i \in CS(V_{\text{ILA}}^{\text{sync}})$, we include both the corresponding call node call_i and return node ret_i in the slice. The final ILA slice is then defined as

$$V_{\text{ILA}}^{\text{final}} = V_{\text{ILA}}^{\text{sync}} \cup \{\text{call}_i, \text{ret}_i \mid i \in CS(V_{\text{ILA}}^{\text{sync}})\}.$$

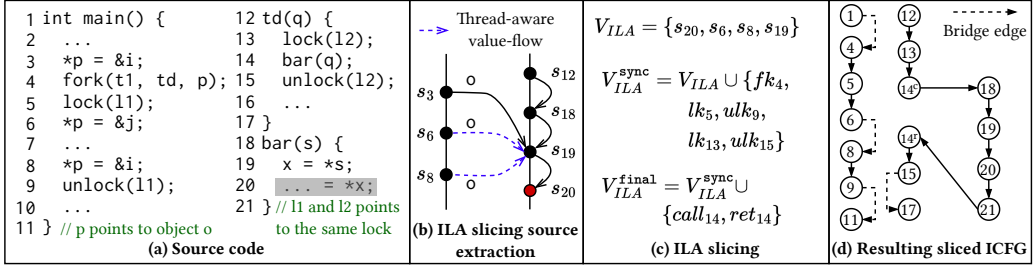


Fig. 8. ILA slicing example.

Sliced ICFG construction. Given the complete set of nodes to be retained, Algorithm 1 first adds the entry and exit nodes of every retained function as context-sensitive propagation boundaries. We use $entry_f \in V'$ to indicate that function f is retained. Its entry and exit nodes are always added together. For each callsite i having a resolved callee f with $entry_f \notin V'$, we seed a paired bridge edge $call_i \rightarrow ret_i$. Here, $Callee(i)$ denotes the set of resolved targets of i , so the existential condition in Algorithm 1 also covers an indirect call with an omitted target.

The remaining bridge edges are constructed by contracting non-retained nodes, but a new bridge can compose only intraprocedural edges in E_{intra} or existing bridge edges. Explicit call and return edges therefore never participate in this contraction. They are copied unchanged when both endpoints are retained, while the seeded $call_i \rightarrow ret_i$ edge summarizes a callee that contains no retained node. Consequently, every bridge stays within one function and cannot combine a call at one callsite with the return of another.

This construction gives an exact path abstraction for realizable paths over retained nodes. A path through an omitted callee projects through its paired call-to-return bridge. All other call and return transitions remain explicit and retain their callsite identities. Conversely, every bridge can be lifted to the corresponding local path or matched call-to-return path in the original ICFG. Since the relevant entry, exit, fork/join, and lock/unlock nodes are retained, this correspondence preserves the dominance, post-dominance, and all-path predicates used by ILA to classify joins and lock-release spans.

Theorem 1 (Correctness of ILA Slicing). Let G be the original ICFG and G' be the sliced ICFG produced by ILA slicing and ICFG reconstruction. For any ILA query whose operands are in V_{ILA} , the ILA result on G' is identical to that on G , satisfying the query preservation property for ILA (Definition 3).

PROOF SKETCH. ILA slicing constructs the final slice V_{ILA}^{final} by closing the initial slicing sources V_{ILA} under two types of dependences: (i) synchronization dependences, which retain all synchronization primitives (fork/join and lock/unlock) that may affect interleaving states and lock-release spans, and (ii) call dependences, which retain the call/return nodes necessary to preserve the calling contexts of the retained primitives and target statements. Graph construction additionally retains the entry and exit nodes of every retained function as propagation boundaries. Together, these steps ensure that every synchronization event and calling-context element that may influence the ILA results for statements in V_{ILA} is represented in the slice.

Algorithm 1 composes only intraprocedural and bridge edges when deleting nodes. Its only initial bridge across an omitted callee connects that callsite to its own return node. Explicit call and return edges are retained unchanged for retained callees. It therefore establishes a projection/lifting correspondence over realizable paths without introducing mismatched returns. Together with the retained entry/exit, synchronization primitives, and calling contexts, this correspondence preserves the all-path predicates used to classify joins and lock-release spans. Consequently, the ILA results

for retained statements remain identical to those on the original ICFG G , satisfying the query preservation property (Definition 3). $\square$

Example 3. Figure 8 illustrates the ILA slicing process. The main function spawns a thread executing td and passes pointer p as an argument. The thread td invokes bar within sp_{l2} , passing q as an argument. Inside bar , statement s_{19} loads the pointer argument, and statement s_{20} dereferences it to access the referenced memory. Pre-analysis identifies s_{20} as a potential race statement. We first construct a thread-aware value-flow graph and slice it according to the criterion in Section 4.3, as shown in Figure 8(b). This retains statements $\{s_3, s_6, s_8, s_{12}, s_{18}, s_{19}, s_{20}\}$, inducing two thread-aware value-flow edges: $s_6 \xrightarrow{o} s_{19}$ and $s_8 \xrightarrow{o} s_{19}$. ILA slicing proceeds in three steps. First, source extraction selects s_{20} via [INIT] and includes s_6, s_8 , and s_{19} via [THREAD-VF] for concurrency queries. Second, synchronization-dependence slicing adds relevant synchronization primitives: $\{fk_4, lk_5, ulk_9, lk_{13}, ulk_{15}\}$. Third, call-dependence slicing recovers calling contexts by adding corresponding call and return nodes (e.g., (14^c) and (14^r)). ICFG reconstruction also retains the entry and exit nodes of $main$, td , and bar . The resulting bar fragment is $call_{14} \rightarrow entry_{bar}(18) \rightarrow s_{19} \rightarrow s_{20} \rightarrow exit_{bar}(21) \rightarrow ret_{14}$. Bridge edges bypass the omitted intraprocedural statements in $main$ and td . Context-sensitive ILA on the sliced graph yields the required concurrency information while preserving results.

4.3 FSPTA Slicing

FSPTA slicing reduces the analysis codebase by retaining only statements that affect the points-to information of target pointers (e.g., those accessed in potential race statements), thereby preserving query results for these variables (Definition 3). This is achieved through data-dependence slicing.

Data dependence slicing. Figure 9 presents the inference rules for data-dependence slicing. Given the slicing targets $RacePair_{pre}$, the [INIT] rule initializes the set V_{FSPTA} with statements that define the pointers accessed by statements in $RacePair_{pre}$. Here, $Def(v)$ denotes the statement that defines variable v , while $Ptr(s)$ denotes the pointer accessed in statement s . Subsequently, the [DATA] rule collects all statements that may influence the final pointer analysis outcome by performing a backward traversal along the data-dependence chain, thereby ensuring that all relevant dependencies are captured.

$$[INIT] \frac{(s, s') \in RacePairs_{pre} \quad v = Ptr(s) \quad v' = Ptr(s')}{\{Def(v), Def(v')\} \subseteq V_{FSPTA}} \quad [DATA] \frac{s \in V_{FSPTA} \quad (s_d, s) \in E_d}{s_d \in V_{FSPTA}}$$

Fig. 9. Inference rules for data dependence slicing.

Definition 4 (Data Dependence). Data dependence is a binary relation E_d over program statements: $(s, s') \in E_d$ if and only if a value defined in statement s is used in statement s' . These data dependencies are inherently represented in the thread-aware value-flow graph, which is constructed using the context-sensitive ILA results from the main analysis phase and the pre-analysis points-to results. Only value flows retained in VFG'_{pre} are considered in the construction of E_d .

Theorem 2 (Correctness of FSPTA Slicing). FSPTA on the sliced program yields the same points-to results for the target variables as on the original program, thereby satisfying the query preservation property for FSPTA (Definition 3).

PROOF SKETCH. FSPTA relies on thread-aware value flows, which depend on ILA results. ILA slicing source extraction (Section 4.2) preserves all statements required for constructing thread-aware value flows: Rule [INIT] includes statements in $RaceStmt_{pre}$, while Rule [THREAD-VF] includes statements queried for ILA information during value-flow construction.

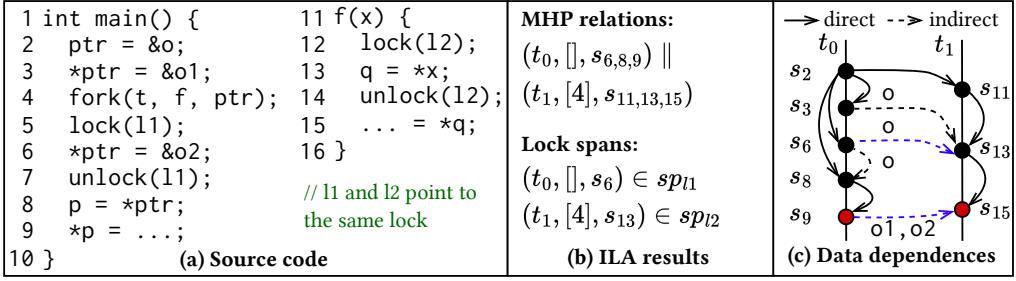


Fig. 10. FSPTA slicing example.

Let VFG denote the original value-flow graph and VFG' the sliced graph. Since VFG_{pre} uses pre-analysis ILA results that over-approximate main-phase results, we have $ThreadVF(VFG') \subseteq ThreadVF(VFG'_{pre})$, ensuring VFG'_{pre} contains all useful thread-aware value flows. For each retained edge $s \xrightarrow{o} s' \in ThreadVF(VFG')$, the set $Query(s \xrightarrow{o} s')$ contains endpoints and intra-span witnesses needed to query ILA results. By Theorem 1, these ILA results are preserved.

Data-dependence slicing constructs V_{FSPTA} by retaining all statements reachable along value flows from the defining statements of target pointers. Since all statements contributing to the points-to relation of target variables are included in V_{FSPTA} , sparse FSPTA on the sliced graph yields identical points-to results, satisfying the query preservation property. $\square$

Example 4. Consider the example in Figure 10, where `main` spawns a thread executing `f` at fk_4 with pointer `ptr`. Pre-analysis identifies a potential race pair $(s_9, s_{15}) \in RacePairs_{pre}$. Using pre-analysis points-to results and context-sensitive ILA results (Figure 10(b)), we construct a thread-aware value-flow graph inducing the data dependencies in Figure 10(c). These dependencies include: (i) direct dependencies (e.g., $s_2 \rightarrow s_3$) from def-use chains of top-level variables, (ii) indirect dependencies (e.g., $s_3 \dashrightarrow s_{13}$) from def-use chains of address-taken variables, and (iii) thread-aware def-use dependencies (e.g., $s_6 \dashrightarrow s_{13}$) capturing inter-thread value flows.

Data-dependence slicing proceeds from the identified race pair as follows. The [INIT] rule initializes V_{FSPTA} with statements defining the accessed pointers (i.e., s_8 and s_{13} for `p` and `q`). The [DATA] rule then extends V_{FSPTA} by backward traversal along data-dependence paths to include all transitively influencing statements. The resulting slice $V_{FSPTA} = \{s_2, s_3, s_6, s_8, s_{11}, s_{13}\}$ is sufficient for preserving the required points-to results of `p` and `q` in the FSPTA phase.

5 Evaluation

In this section, we evaluate our multi-stage slicing approach, focusing on its effectiveness in reducing both the analysis scope and computational cost, while verifying that it preserves precision and soundness. To demonstrate the advantages of our design, we also implement and compare against a straightforward baseline, single-pass slicing, which merges ILA slicing source extraction and FSPTA slicing into a unified pass.

Our evaluation aims to address the following research questions:

- RQ1 Slicing effectiveness:** To what extent does slicing reduce the analysis scope and computational cost for both ILA and FSPTA?
- RQ2 Precision and soundness preservation:** Does slicing preserve the correctness of ILA results (including interleaving analysis and lock analysis) and FSPTA results (alias queries) that are essential for downstream bug detection?
- RQ3 Benefit of multi-stage slicing:** What are the additional advantages of multi-stage slicing over single-pass slicing in terms of analysis scope reduction and overall efficiency?

Table 1. Statistics of 10 open-source projects. *#LOI* denotes the number of lines of LLVM instructions. *#Method*, *#Call*, *#Ptr*, and *#Obj* are the numbers of functions, method calls, pointers, and memory objects, respectively. $|V|$ and $|E|$ are the numbers of ICFG nodes and edges.

Project	<i>#LOI</i>	<i>#Method</i>	<i>#Call</i>	<i>#Ptr</i>	<i>#Obj</i>	$ V $	$ E $
radiosity	14,873	53	631	11,853	163	7,459	8,374
ferret	18,490	58	579	12,528	187	7,938	8,323
bodytrack	21,358	81	627	16,034	212	8,930	9,005
raytrace	106,473	391	4,879	93,617	617	53,762	54,483
x264	147,110	481	5,440	143,325	985	125,571	128,374
httpd	182,833	2,526	7,124	191,051	13,147	172,095	162,743
darknet	213,858	987	9,920	195,684	2,568	135,169	148,925
teeworlds	272,443	2,334	20,590	328,211	5,813	228,395	215,926
NanoMQ	385,737	3,235	39,415	382,746	31,736	313,571	441,396
redis	469,883	6,304	41,097	549,641	9,817	415,349	457,513
Total	1,833,058	16,450	130,302	1,924,690	65,245	1,468,239	1,635,062

5.1 Datasets and Implementation

Datasets. We evaluate MS_{LI} on ten real-world projects spanning diverse application domains. These include five large applications from the PARSEC-3.0 benchmark suite [10]: radiosity (graphics rendering), ferret (content-based similarity search server), bodytrack (computer vision-based body tracking), raytrace (physically-based ray tracing), and x264 (H.264/MPEG-4 AVC video encoding). Additionally, we evaluate five widely-used open-source applications: httpd [4] (Apache HTTP server), darknet [3] (neural network framework for deep learning), teeworlds [2] (online multiplayer game engine), NanoMQ [1] (lightweight MQTT broker for IoT edge platforms), and redis [5] (in-memory key-value database). This diverse selection enables us to assess the effectiveness of MS_{LI} across realistic and heterogeneous concurrent software systems.

Implementation. All experiments are conducted on an Ubuntu 22.04 server equipped with an 8-core 2.60GHz Intel Xeon CPU and 128 GB of memory. We construct interprocedural control-flow graphs (ICFGs) and value-flow graphs (VFGs) from LLVM IR (LLVM 16.0.0) using the SVF library [40] (v3.2). Our slicing implementation is built on top of FSAM, the flow-sensitive analysis module provided by the SVF framework. FSAM provides the flow-insensitive Andersen-style pointer analysis and context-insensitive ILA used in pre-analysis, as well as the main-phase FSPTA and ILA. The main-phase ILA is configured with 3-CFA in both FSAM and MS_{LI}.

5.2 RQ1: Effectiveness in Accelerating Analysis

In this section, we evaluate the extent to which MS_{LI} reduces the analysis scope and accelerates the overall analysis pipeline. Using ten large-scale projects, we first quantify the reduction in analysis scale and the resulting speedups. We then examine the time breakdown across analysis phases to assess the overhead introduced by slicing.

Reduction in analysis scope and cost. Table 2 compares MS_{LI} against FSAM with respect to ICFG size (measured by node and edge counts) and main-phase analysis time, decomposed into ILA, FSPTA, and total execution time. Overall, slicing reduces the ICFG node count to 5.4% for ILA and 25.7% for FSPTA on average, with proportional reductions observed in edge counts. Correspondingly, the runtime for ILA decreases to 4.7% of the baseline, while FSPTA runtime

Table 2. Reduction in analysis scope and speedup achieved by MS_{LI}. ICFG size (node/edge counts) and analysis time are reported for FSAM (without slicing) and MS_{LI} (with slicing), broken down by ILA, FSPTA, and total analysis cost.

Project	FSAM						MSLI					
	Code size		Time (sec)			Code size				Time (sec)		
	V	E	ILA	FSPTA	Tot.	V _{ILA}	E _{ILA}	V _{FSPTA}	E _{FSPTA}	ILA	FSPTA	Tot.
radiosity	7,459	8,374	2.4	2.7	5.3	832	917	4,324	4,389	0.2	1.5	2.6
ferret	7,938	8,323	4.3	3.1	7.9	938	991	3,716	3,861	0.6	1.3	3.5
bodytrack	8,930	9,005	26.3	34.4	62.3	1,465	1,493	4,280	4,331	1.9	3.8	9.9
raytrace	53,762	54,483	84.5	96.3	184.9	2,354	2,404	15,233	15,415	2.7	10.7	26.1
x264	125,571	128,374	153.8	121.5	281.8	3,152	3,387	17,482	17,570	3.1	14.3	39.1
httpd	172,095	162,743	169.4	172.0	351.1	2,164	2,204	20,154	20,648	5.2	18.1	52.3
darknet	135,169	148,925	241.9	191.1	443.8	3,979	4,185	15,628	16,012	7.3	18.5	60.9
teeworlds	228,395	215,926	267.6	318.8	602.7	3,195	3,278	34,254	35,024	6.5	34.6	82.3
NanoMQ	313,571	441,396	304.8	374.5	701.7	3,914	4,116	42,938	43,153	8.4	47.3	117.3
redis	415,349	457,513	671.4	538.4	1,246.7	5,312	5,440	43,841	44,107	10.9	43.5	152.8
Total	1,468,239	1,635,062	1,926.4	1,852.8	3,888.2	27,305	28,415	201,850	204,510	46.8	193.6	546.8

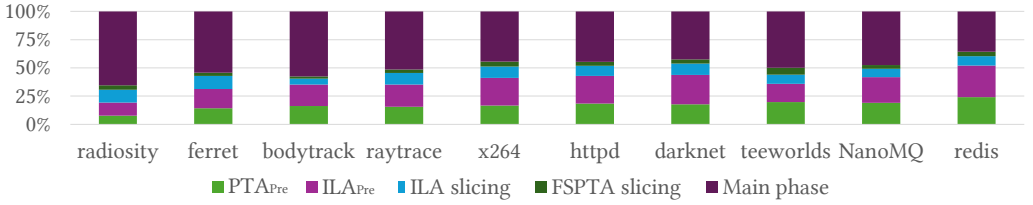


Fig. 11. Time breakdown of MS_{LI} across analysis phases.

decreases to 18.3%, resulting in an overall reduction in total analysis time to 20.8% (achieving as low as 12.3% on redis).

Time breakdown and slicing overhead. Figure 11 presents a detailed breakdown of the execution time of MS_{LI} across different phases, including pre-analysis (PTA_{Pre} and ILA_{Pre}), ILA/FSPTA slicing, and the main-phase analysis. The combined overhead introduced by MS_{LI} (comprising ILA_{Pre} and ILA/FSPTA slicing) accounts for 33.7% of the total analysis time on average, reaching at most 40.2% on radiosity. In contrast, the main phase accounts for 49.3% on average, which is comparable to the pre-analysis phase. This balance is attributable to the substantial acceleration achieved through slicing. These results demonstrate that our approach delivers significant speedup while incurring only modest overhead.

5.3 RQ2: Precision and Soundness

This section evaluates whether MS_{LI} satisfies the query preservation property for ILA and FSPTA (Definition 3). We report results for the two ILA components, interleaving analysis (IA) and lock analysis (LA), as well as FSPTA. For clarity, when the same statement is queried multiple times, we count it only once. The #query values are estimates derived from the artifact, while the #true and Alarms values are analysis results.

Every query answer from FSAM matches the corresponding answer from MS_{LI}. Table 3 reports one set of results. Both analyses also report identical race statements, confirming query preservation on the evaluated benchmarks.

Table 3. Intermediate query results and race alarms. For each analysis, #query is the estimated number of conceptual queries and #true is the number that evaluate to true. FSAM and MS_L return identical answers, so each result is shown once.

Project	IA		LA		FSPTA		Alarms
	#query	#true	#query	#true	#query	#true	
radiosity	255	52	73	17	102	26	10
ferret	238	63	77	21	109	31	13
bodytrack	206	86	70	28	95	42	15
raytrace	674	210	254	65	236	72	20
x264	643	198	243	61	245	70	19
httpd	1131	349	594	128	496	139	30
darknet	3424	1045	1144	275	1043	253	43
teeworlds	3855	1176	1451	308	1021	294	46
NanoMQ	5416	1643	2067	418	1409	389	54
redis	5361	1620	1972	410	1480	385	53
Total	21203	6442	7945	1731	6236	1701	303

5.4 RQ3: Ablation Analysis of Multi-Stage Slicing

This section evaluates the effectiveness of our multi-stage slicing strategy by comparing it against a straightforward baseline. The baseline merges ILA slicing source extraction and FSPTA slicing into a unified pass by computing the transitive closure of all target statements under the combined dependence graph, which we refer to as *single-pass slicing*. We compare the two approaches with respect to slice sizes and the resulting analysis time, measured both for the main analysis phase and for the overall execution.

Figure 12(a) compares the number of retained nodes under our multi-stage slicing approach and the single-pass baseline. Overall, multi-stage slicing reduces the ILA slice to 14.2% of the single-pass baseline on average, while the FSPTA slice is reduced to 82.5%. Figure 12(b) reports the corresponding speedups in analysis time. Compared to single-pass slicing, multi-stage slicing reduces the main-phase runtime to 18.9% for ILA and 68.1% for FSPTA on average, and achieves an overall reduction in total runtime to 54.0% (reaching as low as 48.1% on NanoMQ). These results demonstrate that the multi-stage slicing strategy yields substantial additional reductions in both slice size and analysis time, thereby confirming the effectiveness of our multi-stage design.

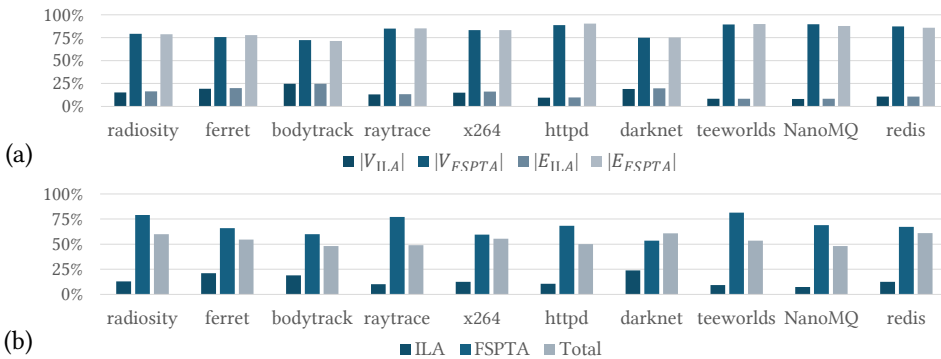


Fig. 12. Normalized MS_L results relative to single-pass slicing for (a) retained ICFG vertices and edges in the ILA and FSPTA slices and (b) ILA, FSPTA, and total analysis time.

6 Related Work

Static analysis for multi-threaded programs. Flow-sensitive pointer analysis [9, 12, 23, 27, 35, 37, 40] typically achieves higher precision than flow-insensitive alternatives by tracking how pointer values evolve along different program control points. Sparse analyses [23, 24, 40] accelerate data-flow resolution by avoiding redundant propagation, with further speedups achieved through object versioning [9] and saturation techniques [47]. In multi-threaded settings, flow sensitivity introduces the additional challenge of reasoning about inter-thread interference. Rugina and Rinard [35] proposed an interprocedural, flow- and context-sensitive pointer analysis for multi-threaded programs. Sui et al. [39] extended sparse FSPTA to multi-threaded C programs, while Cai et al. [12, 51] presented Canary, which leverages thread-modular value-flow analysis and SMT-based constraint solving for concurrency bug detection.

Concurrency analysis for multi-threaded programs [11, 17, 18, 20, 33, 54] underpins downstream tasks such as data race detection [13, 22, 26, 29]. Key advances in May-Happen-in-Parallel (MHP) analysis include region-based approaches for Pthreads [18] and static vector clocks [54]. Additional research addresses language-specific concurrency modeling [21, 41], downstream analysis improvements [27, 30, 36], and hybrid static-dynamic techniques [8]. While prior efforts primarily focus on algorithmic advances for scalability and precision, our work pursues a complementary direction: reducing analysis scope via program slicing. Our approach is agnostic to the specific ILA or FSPTA algorithm employed and serves as a front end that reduces runtime overhead while preserving the precision and soundness of target query results.

Program slicing and staged analysis. Program slicing [25, 43, 46, 48, 49] is a fundamental technique in software engineering and program analysis, widely used for debugging, testing, and static analysis. Considerable effort has been devoted to precise dynamic slicing [6, 45, 53], but dynamic slicing is inherently execution-dependent and thus does not provide the sound, all-path guarantees typically desired in static settings [15, 25, 34]. In contrast, static slicing is defined over program dependences, most notably data and control dependences [25, 43, 46, 48, 52], and has been extensively studied as a foundation for analysis reduction.

Slicing concurrent programs introduces additional challenges due to interference across threads. Nanda et al. [31, 32] address this by proposing context-sensitive interference dependences, and subsequent work (e.g., by Krinke [28]) further advances concurrency-aware slicing. These approaches primarily target general-purpose slicing criteria, rather than explicitly guaranteeing the preservation of specific static-analysis results (e.g., MHP/lock predicates or alias queries) for downstream analyses. Several analyses use a lightweight preliminary analysis to guide a more precise subsequent phase [16, 39, 44]. Other techniques use static reduction or slicing to limit the scope of testing or analysis [14, 19, 38]. For instance, Cheng et al. [16] use path-insensitive results to accelerate path-sensitive analysis, while Chebaro et al. [14] leverage static analysis to speed up testing. Unlike prior reduction and slicing techniques that compute a single slice for one subsequent analysis, our approach performs multi-stage slicing tailored to the distinct requirements of ILA and FSPTA, preserving precision and soundness for downstream tasks.

7 Conclusion

This paper presents MSLI, a multi-stage slicing framework that improves the scalability of precise analysis for concurrent programs by tailoring program slices to the distinct needs of ILA and FSPTA while preserving downstream query results. MSLI uses lightweight pre-analysis to derive over-approximate inter-thread value flows and perform ILA slicing source extraction, then leverages refined ILA results to reconstruct thread-aware value-flow graphs that guide FSPTA-oriented slicing. On ten large real-world projects, MSLI reduces the ICFG to 5.4% for ILA and 25.7% for FSPTA, cuts

total runtime to 20.8% on average, and matches the baseline's ILA/FSPTA query outcomes and race alarms.

Acknowledgments

We thank the anonymous reviewers for their reviews and valuable suggestions. This research is supported in part by the Macquarie University Jumpstart Scheme 531117734 and Australian Research Council Grant DP250101396. We acknowledge the use of the generative AI tool ChatGPT and Claude for language polishing, phrasing and grammar checks. All scientific content, evaluation, and claims are the authors' own.

Data Availability Statement

Our artifact, including implementation and dataset, is available [50]. The up-to-date implementation has also been merged into the SVF framework and is available at <https://github.com/SVF-tools/SVF>.

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Received 2026-01-30; accepted 2026-04-16